




Rock Physics Interpretation of microstructure
Chapter 2.1-2.2-2.3

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- **Introduction**
 - **Theory and models**
 - **Example in North Sea**



Introduction

-- Theoretical models

- Inclusion models
- Contact models
- Computational models
- Bounds
- Transformations

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- Introduction
 - **Theory and models**
 - Example in North Sea

Models for Clay increase

- The friable – sand model
- The contact- cement model
- The constant-cement model

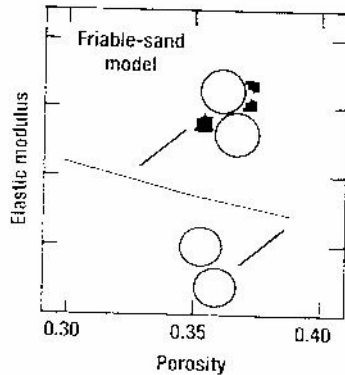
Models for shales

- The constant-clay model for sandy shale
- Dvorkin-Gutierrez silty shale model
- Yin-Marion silty shale model

Models for shaly sands

- The constant-clay model for shaly sands
- Yin-Marion shaly sand model
- Dvorkin-Gutierrez shaly sand model
- Jizba's cemented shaly sand model

The friable – sand model

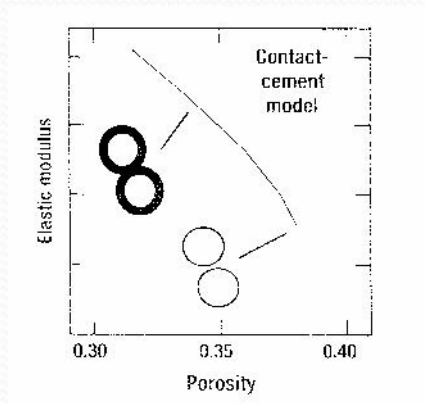


Adding smaller clay deposited in the pore space, deteriorate sorting, decrease porosity, slightly increase the stiffness

\emptyset_c is the point divide the two end member, around \emptyset_c , use Hertz-Mindlin theory to calculate dry rock bulk and shear moduli.

Around zero porosity, use Hashin-Shtrikman bound to calculate dry rock bulk and shear moduli.

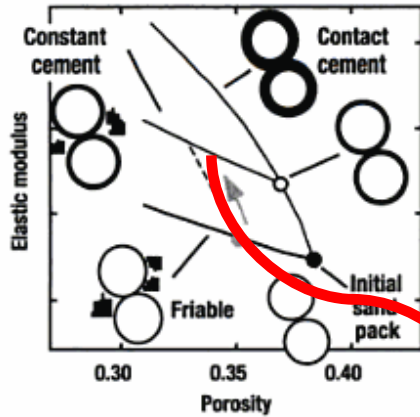
The contact- cement model



clay deposited at the crack spaces near the grain contacts, so the stiffness of rock rapidly increase with very little change in porosity.

This mathematical model is soluted by Dvorkin et al, to get the day bulk and shear moduli.

The constant-cement model



Assume that sands of varying sorting, all have the same amount of contact cement, porosity reduction is solely due to noncontact pore-filling material.

First get the well-sorted end-member porosity Φ_b

The equation for dry-rock bulk and shear moduli at a smaller porosity see Page 58

Models for shales

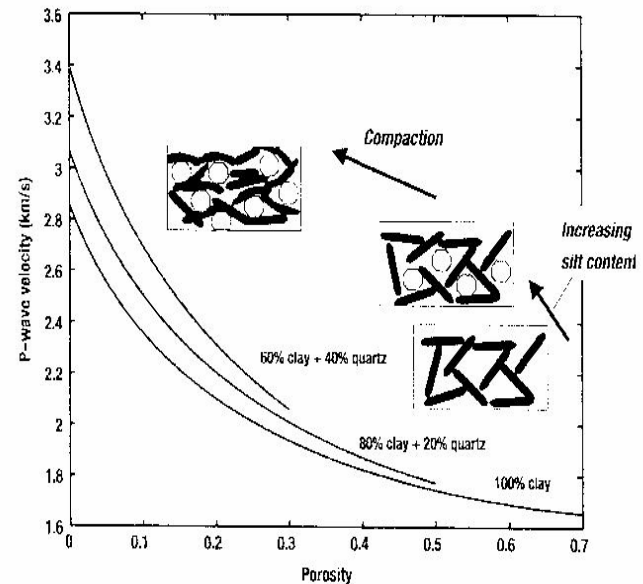
--shale is a sheet like structure and bound water

- The constant-clay model for sandy shale
- Dvorkin-Gutierrez silty shale model
- Yin-Marion silty shale model

The constant-clay model for sandy shale
silt grains are suspended in the shale matrix

Dvorkin-Gutierrez silty shale model
Model the velocity-porosity trend of decreasing clay content

Yin-Marion silty shale model
Use the Reuss bound to calculate the elastic moduli of shales with dispersed quartz grains



Models for shaly sands

--slope of v - \emptyset in sandstone depends largely on the geologic processing porosity variations controlled by diagenesis

- The constant-clay model for shaly sands
- Yin-Marion shaly sand model
- Dvorkin-Gutierrez shaly sand model
- Jizba's cemented shaly sand model
- The laminated sand-shale model

The constant-clay model for shaly sands

Constant clay-quartz ratio

High \emptyset --- function of clay content

Low \emptyset --- function of quartz and clay

The constant-clay lines are calculation equations

$$K_{\text{mixed}} = (1-C)K_{\text{qz}} + CK_{\text{clay}}$$

$$\mu_{\text{mixed}} = (1-C)\mu_{\text{qz}} + C\mu_{\text{clay}}$$

$$\rho_b = \Phi\rho_{\text{fl}} + (1-\Phi)\rho_{\text{min}}$$

Yin-Marion shaly sand model

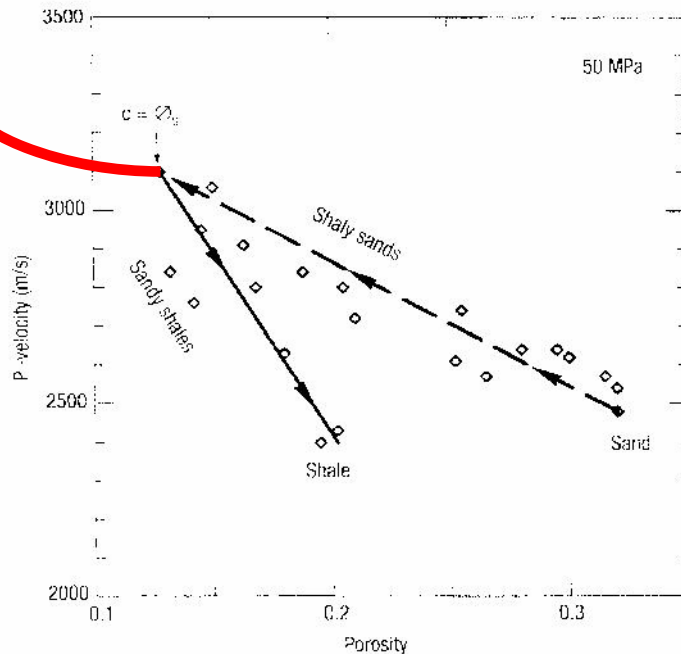
in unconsolidated rock, increasing clay content (C), then total porosity will
Decrease linearly.

$$\Phi = \Phi_s - C(1 - \Phi_{sh}), \text{ for } C < \Phi_s$$

$$\Phi = \Phi_s \Phi_{sh}, \text{ for } C = \Phi_s$$

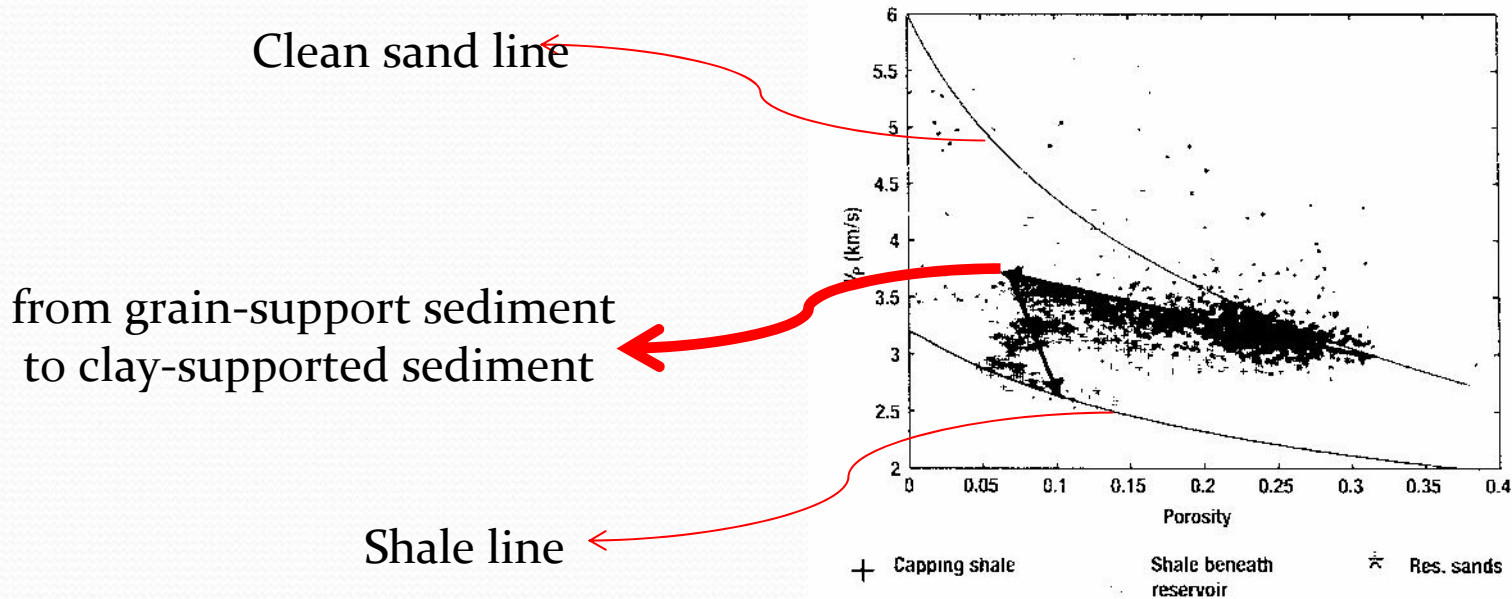
$$\Phi = \Phi_{sh} C, \text{ for } C > \Phi_s, \text{ intrinsic clay } \Phi$$

For calculation, use
Gassman
to replace porous fluids
with
pore-filling clay



Dvorkin-Gutierrez shaly sand model

Instead of using Gassmann theory, we can use the lower bound Hashin-Shtrikman to calculate velocity-porosity trends for sands with increasing clay content
Formula see page66

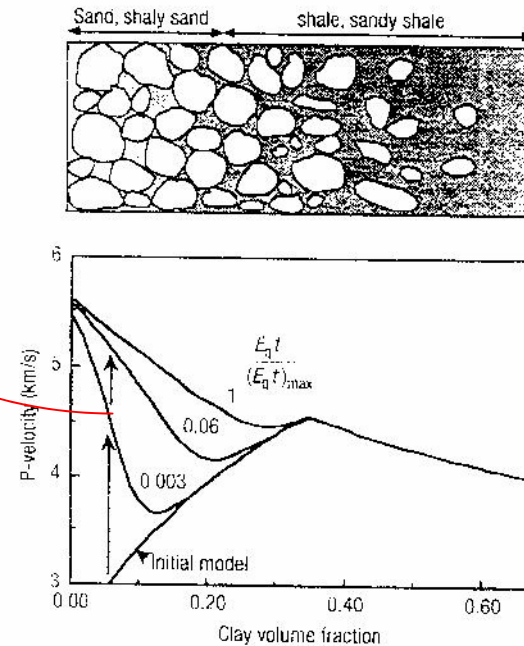


Jizba's cemented shaly sand model

The model same with Yin-Marion shaly sand model, just considered quartz(function of clay content) **cementation**

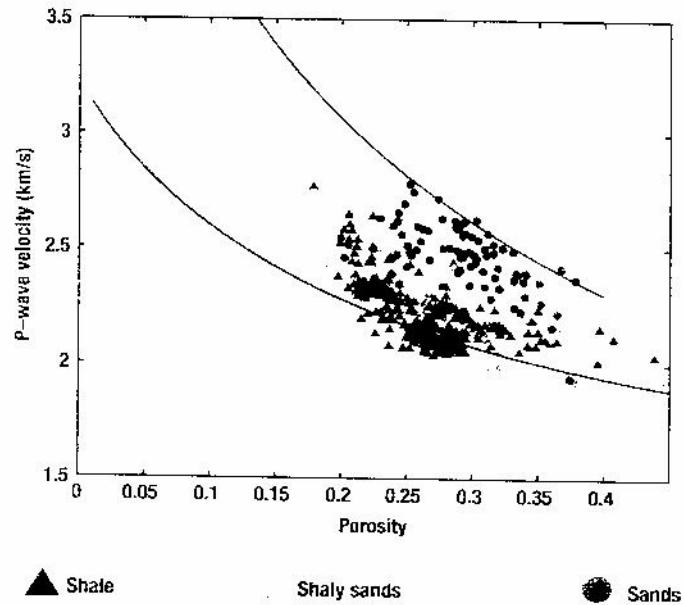
Empirical equation $V-\emptyset$ --- function of quartz volume and clay content


Those curves represent increasing degree of diagenesis as indicated by the elapsed time E_{qt}



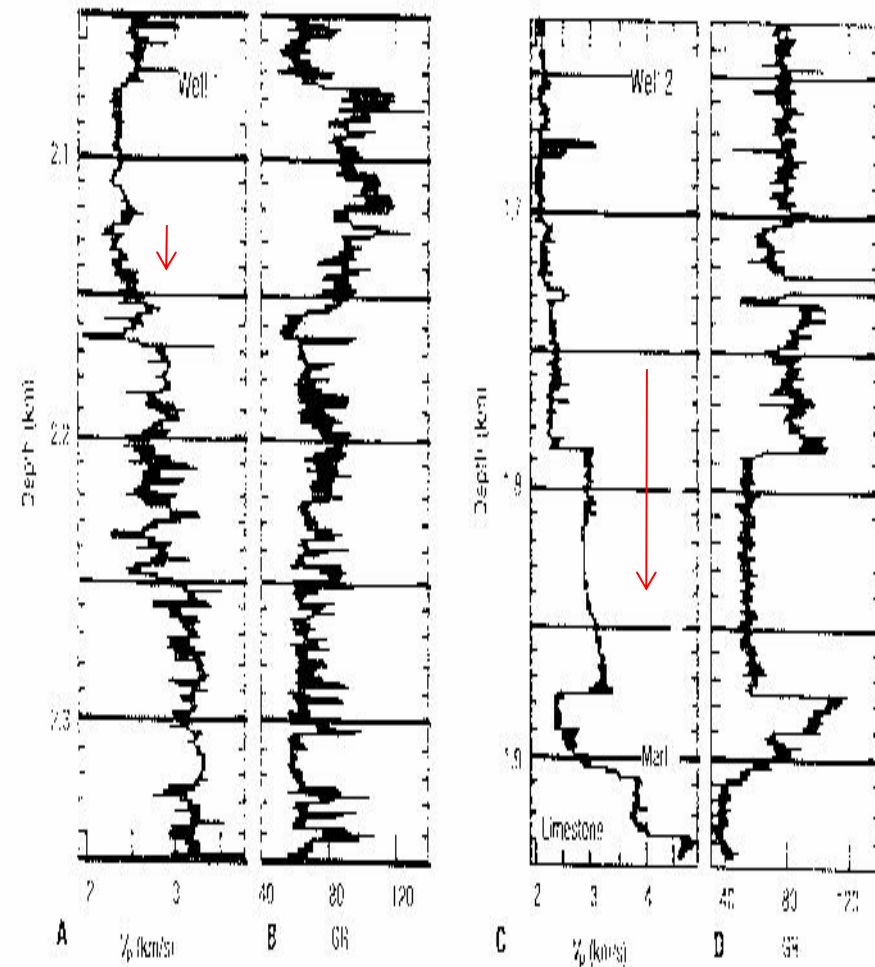
The laminated sand-shale model

‘it is a gradual spread from clean sands via shaly sand to shales, porosity-independent transition with increasing clay content, the shaly sands to be laminated sand-shale unit’

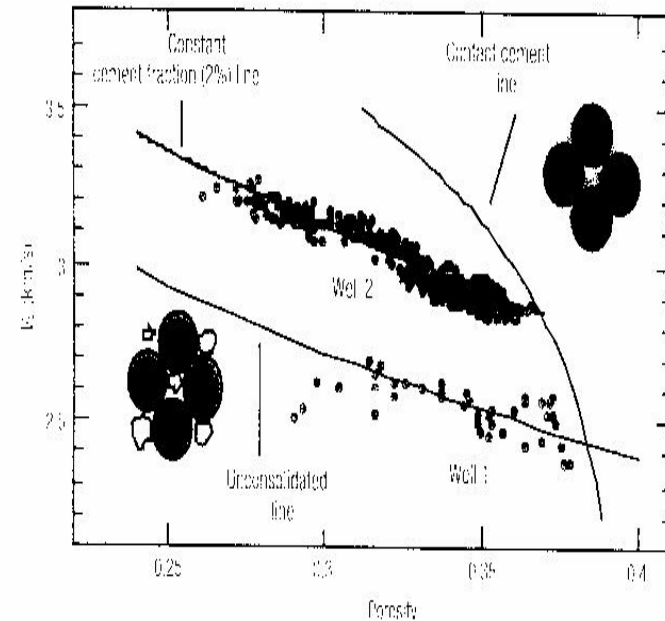
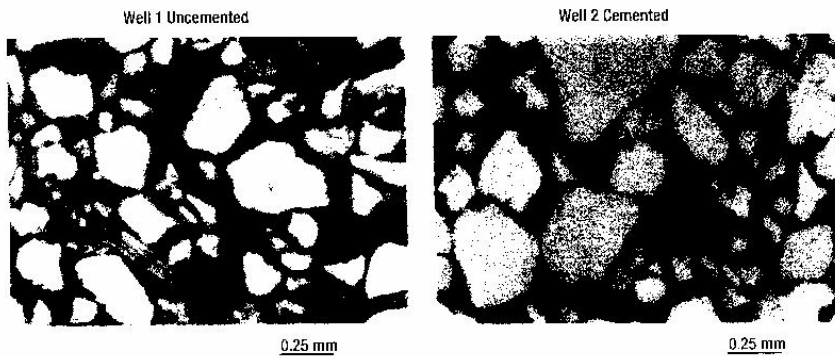


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Both wells represent the same stratigraphic unit, the **pay zones** are marked by **red arrows**.

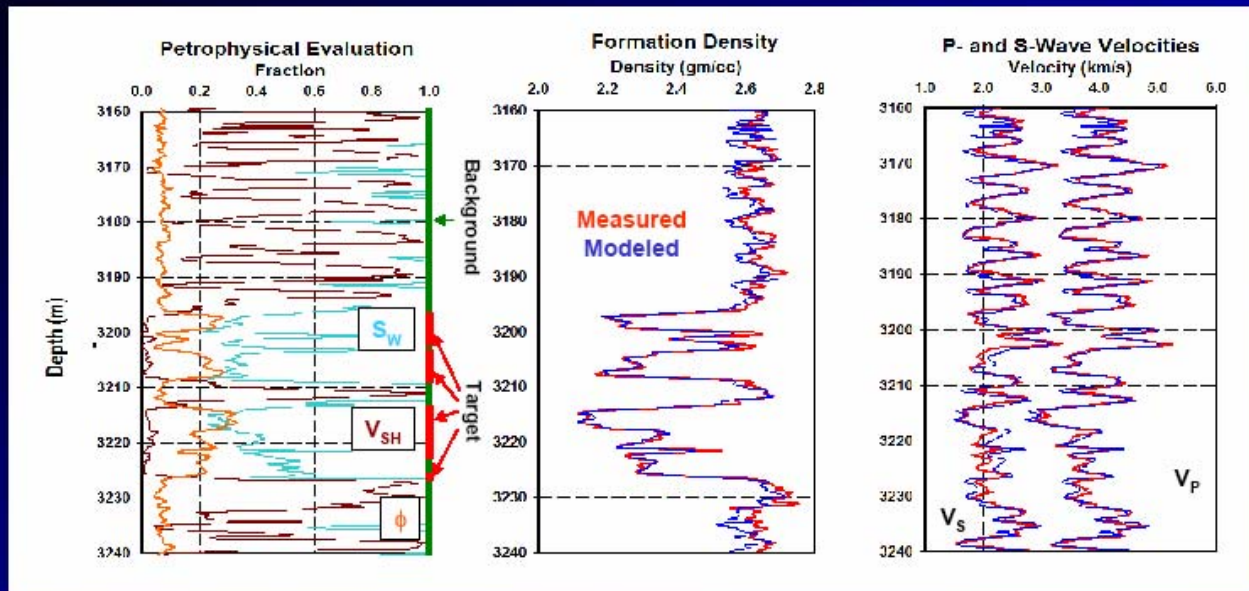


Why the velocity difference in the two wells of the pay zones?



well 1 **small** reducing porosity because of smaller grains deposite on the contact area, this sand has no contact cementation.

well 2 sand has initial contact cementation, so smaller grains fall in the pore space and have **larger** effect on the porosity.



Alvaro, 2007

From Fred J. Hilterman

Building Velocity vs Porosity

Depositional Rock-Property Template

Computations for new porosity value

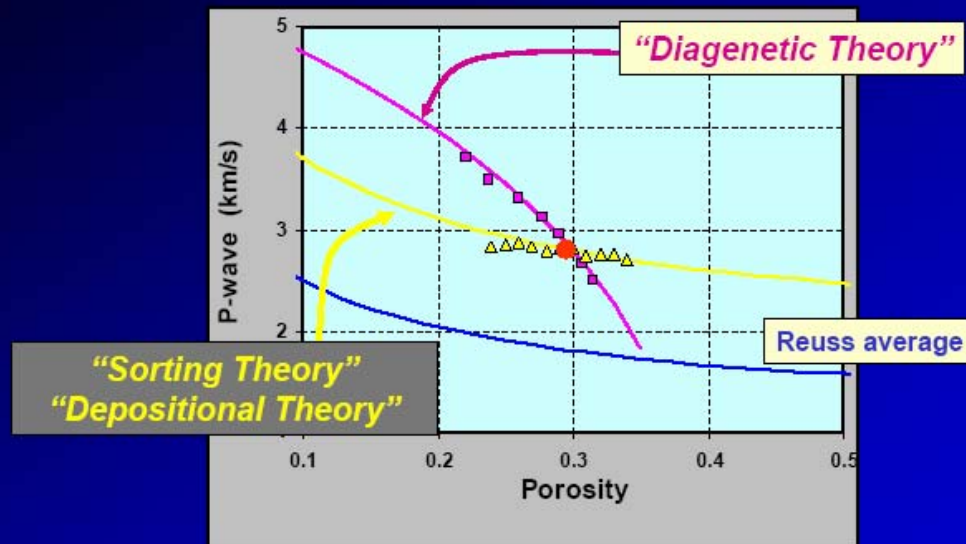
- Rock density
- K_{DRY} using seed point K_{PORE}
- μ_{SAT} using seed point ratio $K_{\text{DRY}} / \mu_{\text{SAT}}$
- K_{SAT} using Gassmann equation
- P-wave velocity

Diagenetic Rock-Property Template

Computations for new porosity value

- Rock density
- K_{DRY} using critical porosity
- μ_{SAT} using seed point ratio $K_{\text{DRY}} / \mu_{\text{SAT}}$
- K_{SAT} using Gassmann equation
- P-wave velocity

Velocity vs Porosity Cross Plot Theory vs Field Data

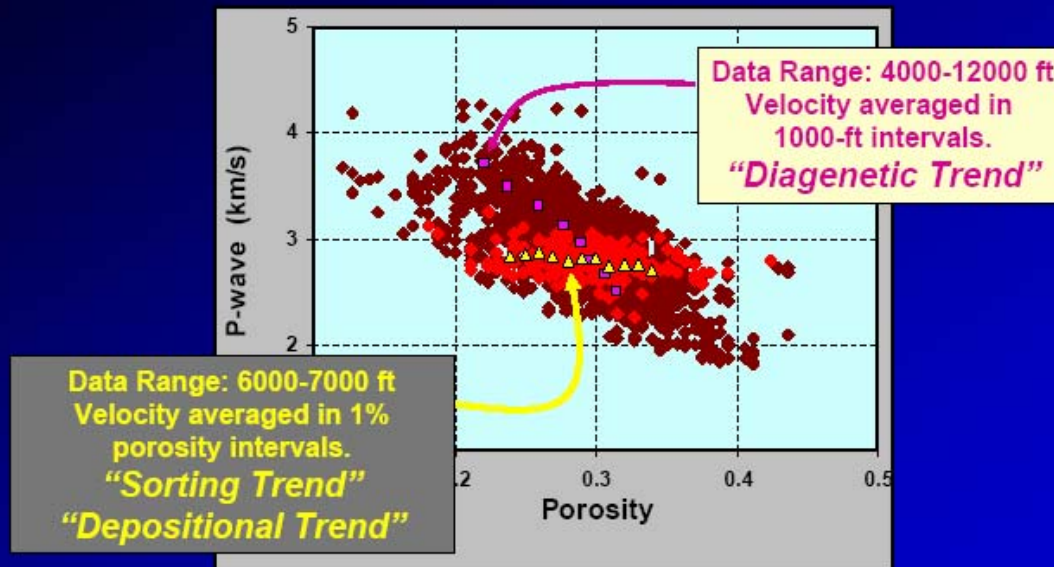


Theoretical *diagenetic* and *depositional* curves match field trends.

From Fred J. Hilterman

Velocity vs Porosity

Depositional and Diagenetic Trends from Field Data



◆ Sample depth range from 700 – 12000 ft

◆ Sample depth range from 6000-7000 ft